

Rossella Carrato - MAT

Homework - ARITMETIC

ESERCIZIO 2

Quanti termini sono necessari per ottenere in precisione ϵ la funzione $f(x) = \cos x$ su tutto $[0, \pi]$?

Formula di Taylor: $x \approx x_0$

$$f(x) = f(x_0) + f'(x_0)(x-x_0) + \frac{f''(x_0)}{2!}(x-x_0)^2 + \dots + \frac{f^{(n)}(x_0)}{n!}(x-x_0)^n + \underbrace{\frac{(x-x_0)^{n+1}}{(n+1)!} f^{(n+1)}(\xi)}$$

$$m = n + 1 \quad \Rightarrow \quad R_m \equiv \frac{1}{m!} (x-x_0)^m$$

$$m = 2 \Rightarrow R_m \cong \cdot 31 >$$

$$m = 3 \Rightarrow R_m \cong 8.1 \times 10$$

$$m = 4 \Rightarrow R_m \cong 1.6 \times$$

$$m = 5 \Rightarrow R_m \cong 2.5 \times$$

$$m = 6 \Rightarrow R_m \cong 3.3 \times$$

$$m = 7 \Rightarrow R_m \cong 3.4 \times$$

$$m = 8 \Rightarrow R_m \cong 3.6 \times$$

$$m = 9 \Rightarrow R_m \cong 3.1 \times$$

\leadsto Mi basta che $m = 9$

che il polinomio di T

almeno 8.

ESERCIZIO 3

ESERCIZIO 14

$$(7316)_8 \rightarrow (?)_2$$

$$\begin{aligned} (7316)_8 &= 7 \times (2^3) + 3 \times (2^2) + 1 \times (2^1) + 6 \times (2^0) \\ &= (111)_2 \times 2^3 + (011)_2 \times 2^2 + (001)_2 \times 2^1 + (100)_2 \times 2^0 \\ &= (11101101)_2 \end{aligned}$$

$$\begin{array}{r|l} :2 & \\ 7 & 1 \\ 3 & 1 \\ 1 & 1 \\ 0 & \end{array}$$

$$\begin{array}{r|l} :2 & \\ 3 & 1 \\ 1 & 1 \\ 0 & \end{array}$$

$$\begin{array}{r|l} :2 & \\ 6 & 0 \\ 3 & 1 \\ 1 & 1 \\ 0 & \end{array}$$

ESERCIZIO 15

Calcolare
per memo
con ma

$$(.1)_{10} = (.1100)_2 \times 2^1$$

$$= (2^{-16} + 2^{-20} + 2^{-24} + \dots)$$

$$= 2^{-16} (2^0 + 2^{-4} + 2^{-8} + \dots)$$

$$\sum_{k=0}^{\infty} (2^{-4})^k$$

$$= \frac{2^{-16}}{1 - 2^{-4}} + \frac{2^{-14}}{1 - 2^{-4}} =$$

$$= \frac{1}{61440} + \frac{1}{122880}$$