

# Lesson 14

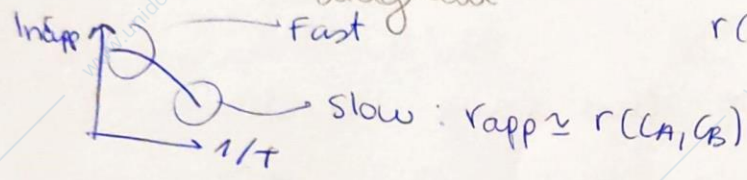
The Kolmogorov scale  $\lambda$  is dependent on the viscosity  $\nu^{3/4}$ .  
 And the  $t_{tr}$  (micromixing time scale) depends on  $\lambda^2$  and overall to the viscosity  $\nu^{1.5}$ .

## Fast reaction rate

It will be reactions that are very fast and inevitably we will have  $Da_{tr} \gg 1$  ( $t_{tr} \ll t_{cr}$ ) so we are in a macromixed space. So the reaction is dominated ~~not~~ by an apparent kinetic which is dominated by the diffusional process.

$$r_{app} \approx \frac{D}{\lambda^2} \cdot C_A$$

## Arrhenius diagram



$$r(C_A, C_B) = k_0 e^{-\frac{E_a}{RT}} \cdot f(C_A, C_B)$$

# Axial dispersion model

molar flux of a compound  $N(z) = \underbrace{UC}_{\text{convective term}} - \underbrace{D \frac{dC}{dz}}_{\text{dispersion term}}$

*mean velocity*

diffusion  $\rightarrow$  individual molecules wavers because of a gradient concentration.

dispersion  $\rightarrow$  fluid packets that due to the turbulent nature of the flow (eddies) will move in different directions, and each packet brings itself all his content.

we can analyze which term <sup>is</sup> more relevant.

axial dispersion time  $t_D = \frac{L^2}{D}$       convective time  $t_C = \frac{L}{U}$

Peclet number  $Pe = \frac{t_D}{t_C} = \frac{UL}{D}$

- when  $Pe \rightarrow 0$ , this mean slow flow with large eddies good mixing to dispersion  $\rightarrow$  CSTR
  - when  $Pe \rightarrow \infty$ , dispersion is negligible
- Lower  $Pe$ , more dispersion strength

we can obtain Pe from the RTD, for example if we put an impulsive tracer on a PFR we obtain the dirac function  $\uparrow \uparrow$ . So, a different response to that one is due to dispersion and we can measure it.

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1) Pe from RTD.

If we add  $H_2$  and PAH, in the diffusion case we will have at the exit  $H_2$  before PAH because it has bigger diffusivity due to its weight. On dispersion is different, we will have  $H_2 + PAH$  at the same time because the eddies moves all together.

Reactor tracing

We have a equation to solve and some boundary conditions (adimensional).

$$\frac{\partial c^*}{\partial \theta} + \frac{\partial c^*}{\partial x} = \frac{1}{Pe} \frac{\partial^2 c^*}{\partial x^2}$$

$$\theta = \frac{t}{\tau} \quad x = \frac{z}{L} \quad c^* = \frac{C}{C_0}$$

We have two processes in parallel, the theoretical model and the experimental data.

$$E_{\theta} = E_{\theta}(\theta, Pe)$$

The two converge when thanks to non linear regression analysis we minimize the deviation.

$$\min \sum_i (E_{\theta, th}(\theta_i) - E_{\theta, exp}(\theta_i))^2 \Rightarrow Pe$$

We need a first guess for Pe. And anyway not always we get a result.

So, we propose other method  $\rightarrow$  van der Laan

Using Laplace we reduce the order of the equation.

$$sC^* + \frac{dC^*}{dx} = \frac{1}{Pe} \frac{d^2C^*}{dx^2}$$

Analogy: ~~for~~

$$\frac{-dC^*}{ds} \Big|_{s=0} = \bar{\theta} = \frac{\tau}{t} \quad \text{first moment}$$

$$\sigma_{\theta}^2 = \frac{\sigma_z^2}{t^2} \quad \text{second moment}$$

We can establish the relationship between  $\sigma_{\theta}^2 \rightarrow Pe$  we have a tool to relate the theoretical model in the Laplace domain with the  $\sigma_{\theta}^2$  of the real reactor (experiment).

Usefull because :

1. We can do it without the non linear regression.
2. without going back from Laplace to time domain.

The adimensional moments are :

titolo  
bar  $\bar{\theta} = \int_0^{+\infty} \theta E(\theta) d\theta$

sigma square  $\sigma_{\theta}^2 = \int_0^{+\infty} (\theta - \bar{\theta})^2 E(\theta) d\theta$

If the vessels is close  $\bar{\theta}$  don't depend on Peclet number and for the other cases the dependence is not strong.

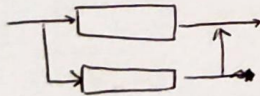
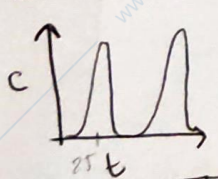
So, we will use  $\sigma_{\theta}^2$  and matching with the experimental result.

For small deviations from ideal flow ( $Pe \rightarrow +\infty$ , PFR) we have that :

$\bar{\theta} = 1$  ,  $\sigma_{\theta}^2 = \frac{2}{Pe}$  from  $Pe \approx 40-50$

Lesson 16 parte 2 no profesor

Esempio 12.2



$E(t) = \frac{Q_1}{Q} \delta(t - \tau_1) + \frac{Q_2}{Q} \delta(t - \tau_2)$

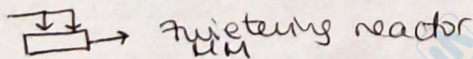
$\tau_1 = \frac{V_1}{Q_1} = 0.25 \text{ min}$

$\frac{Q_1}{Q} = \frac{A_1}{A_1 + A_2} = 0.4$  ,  $V_1 = Q_1 \tau_1 = 0.1 \text{ m}^3$

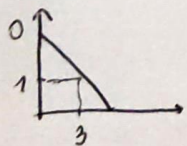
$V_2 = 0.9 \text{ m}^3$

1 m<sup>3</sup> V no dead zones.

2. Also 12.3



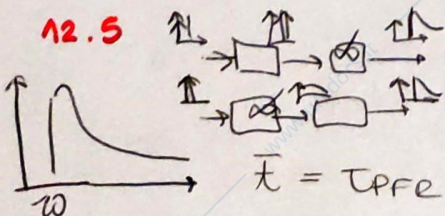
$t > \tau$  mean residence time > space time



- o  $V$  or  $Q$  not correct
- o no proper tracer
- o no closed vessel

CSTR  $\begin{cases} C = A \exp\left(-\frac{t}{\tau_{CSTR}}\right) \\ \log C = \log A - \frac{t}{\tau_{CSTR}} \log e \end{cases}$

12.5



$E(t) = \frac{1}{\tau_{CSTR}} \exp\left(-\frac{t - \tau_{PFR}}{\tau_{CSTR}}\right) u(t - \tau_{PFR})$

$\bar{t} = \tau_{PFR} + \tau_{CSTR} = 50 \text{ s}$

$\bar{t} \neq \tau$  dead zones !!

$V_{dead} = V - V_{CSTR} - V_{PFR} = V - Q \tau_{CSTR} - Q \tau_{PFR} = \square$