

# ESERCITAZIONE SUL CONTROLLO DI PROCESSI TERMO-IDRAULICI

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## - MODELLO NON LINEARE

- CONS. MASSA SERBATOIO:

$$\dot{m} = W - W_0$$

$$z_c + \frac{p_c}{\rho g} = z_c$$

- CONS. Q. DI MOTO CONDOTTA

$$\dot{W} = - \frac{\rho A_c g}{L} (z_c^* - z_v^*)$$

$$z_v + \frac{p_v}{\rho g}$$

- VALVOLA:  $W = k A_v x \sqrt{\rho(p - p_v)}$

$$p_v = p - \frac{W^2}{k^2 A_v^2 x^2 \rho}$$

$$\dot{W} = - \frac{\rho A_c g}{L} \left( z_c - z_v - \frac{p_v}{\rho g} \right) = \frac{\rho A_c g}{L} (z_v - z_c) + \frac{A_c}{L} p_v =$$

$$= \frac{\rho A_c g}{L} (z_v - z_c) + \frac{A_c}{L} p - \frac{A_c W^2}{L k^2 A_v^2 x^2 \rho}$$

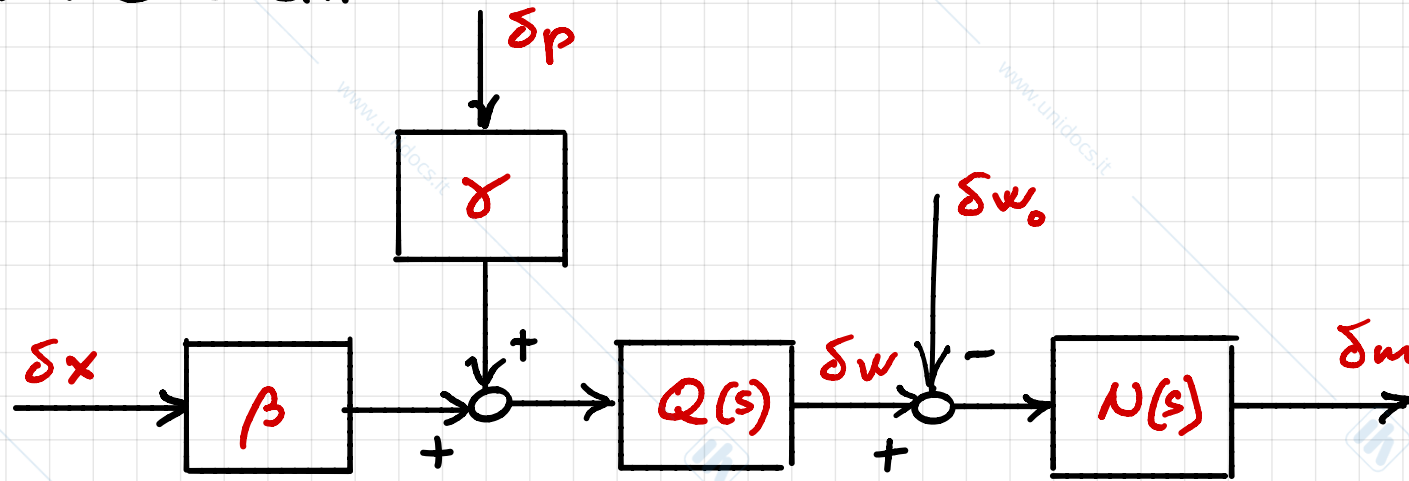
## - MODELLO LINEARIZZATO

$$\begin{cases} \dot{m} = w - w_0 \\ \dot{w} = \frac{\rho A_c g}{L} (z_v - z_c) + \frac{A_c}{L} p - \frac{A_c w^2}{L k^2 A_v^2 x^2 g} \end{cases}$$

$$\begin{cases} \delta \dot{m} = \delta w - \delta w_0 \\ \delta \dot{w} = - \underbrace{\frac{2A_c}{L} \frac{\bar{w}}{k^2 A_v^2 \bar{x}^2 g}}_{\alpha} \delta w + \underbrace{\frac{A_c}{L}}_{\gamma} \delta p + \underbrace{\frac{2A_c}{L} \frac{\bar{w}^2}{k^2 A_v^2 \bar{x}^3 g}}_{\beta} \delta x \end{cases}$$

$$\begin{cases} M(s) = \frac{1}{s} (W(s) - W_0(s)) \\ W(s) = \frac{1}{s + \alpha} (\beta X(s) + \gamma P(s)) \end{cases}$$

## - SCHEMA A BLOCCHI

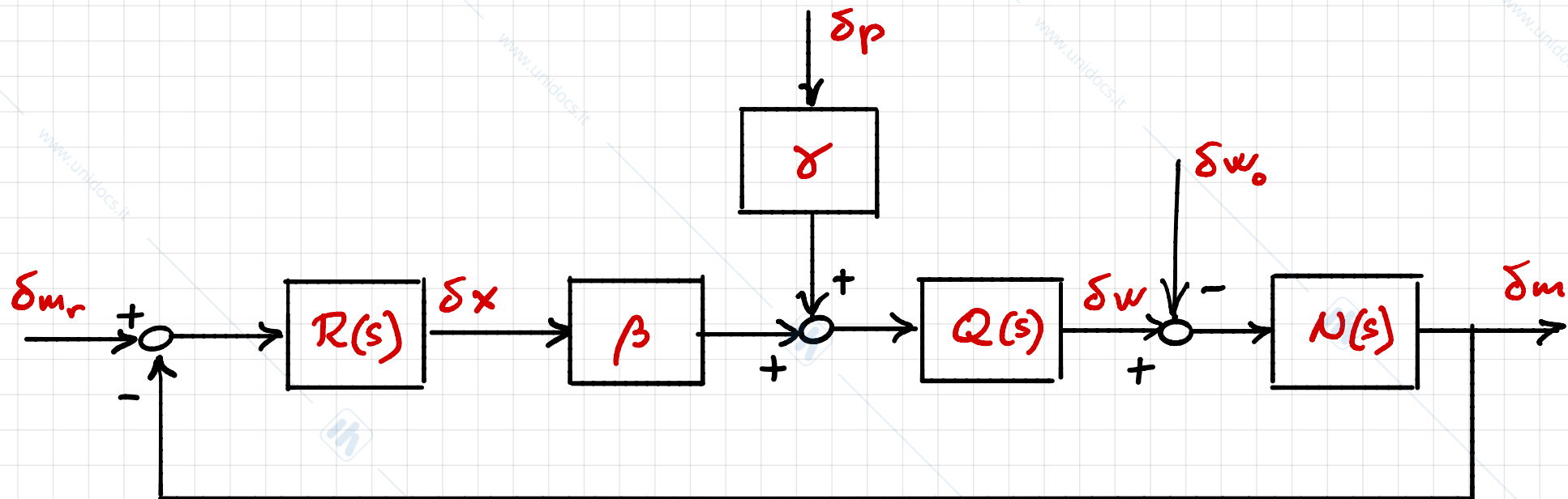


$$Q(s) = \frac{1}{s + \alpha}$$

$$N(s) = \frac{1}{s}$$

$$\alpha, \beta, \gamma > 0$$

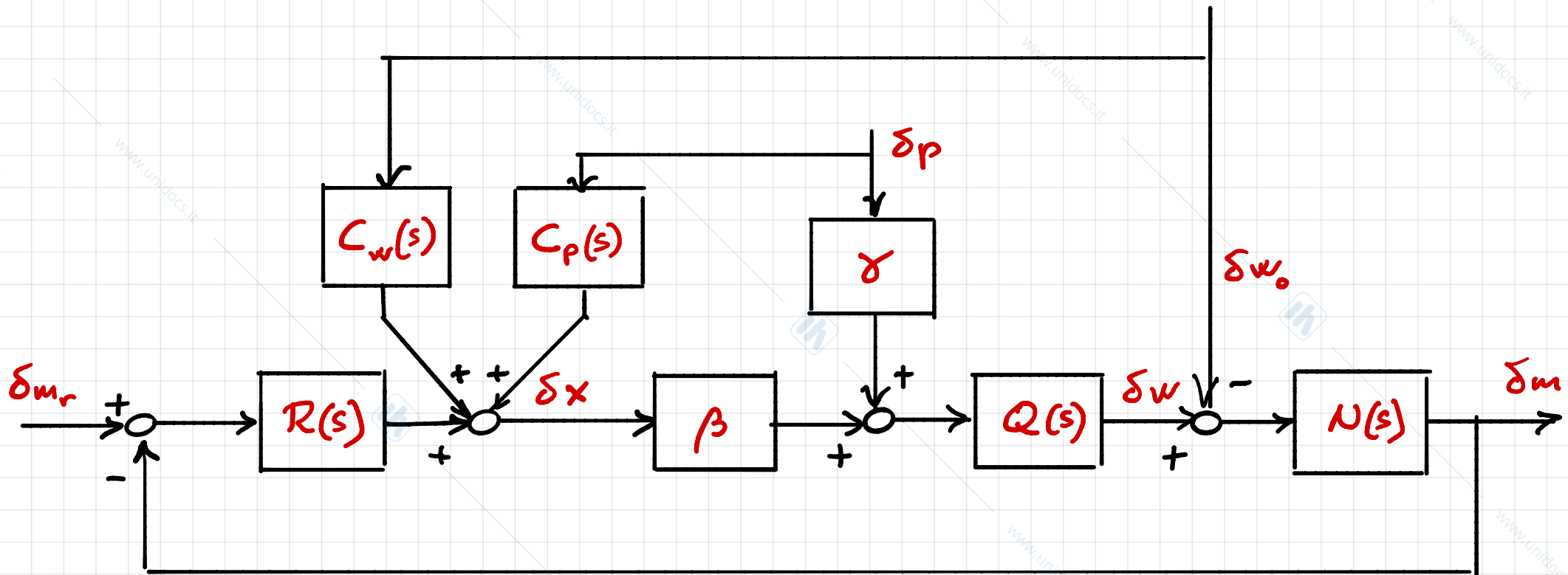
## • PROGETTO DI UN CONTROLLORE DI MASSA



$R(s)$  PROGETTATO SU  $G_{mx}(s) = \beta Q(s) N(s) = \frac{\beta}{s(s+\alpha)}$

- DEVE AVERE AZIONE INTEGRALE (PER DISTURBI  $\delta p, \delta w_0$ )
- DEVE AVERE GUADAGNO POSITIVO PER LA STABILITÀ
- POTREBBE AVERE UNO ZERO CON  $T = \frac{1}{\alpha}$  PER CANCELLARE IL POLO, E UN ALTRO ZERO PER L'ASINTOTICA STABILITÀ

# - COMPENSAZIONE IN A.A. DEI DISTURBI



$$C_p(s) = -\frac{\gamma}{\beta} = -\frac{k^2 A_v^2 \omega^{-3}}{2\omega^2}$$

$$C_w^0(s) = \frac{1}{\beta Q(s)} = \frac{s+\alpha}{\beta}$$

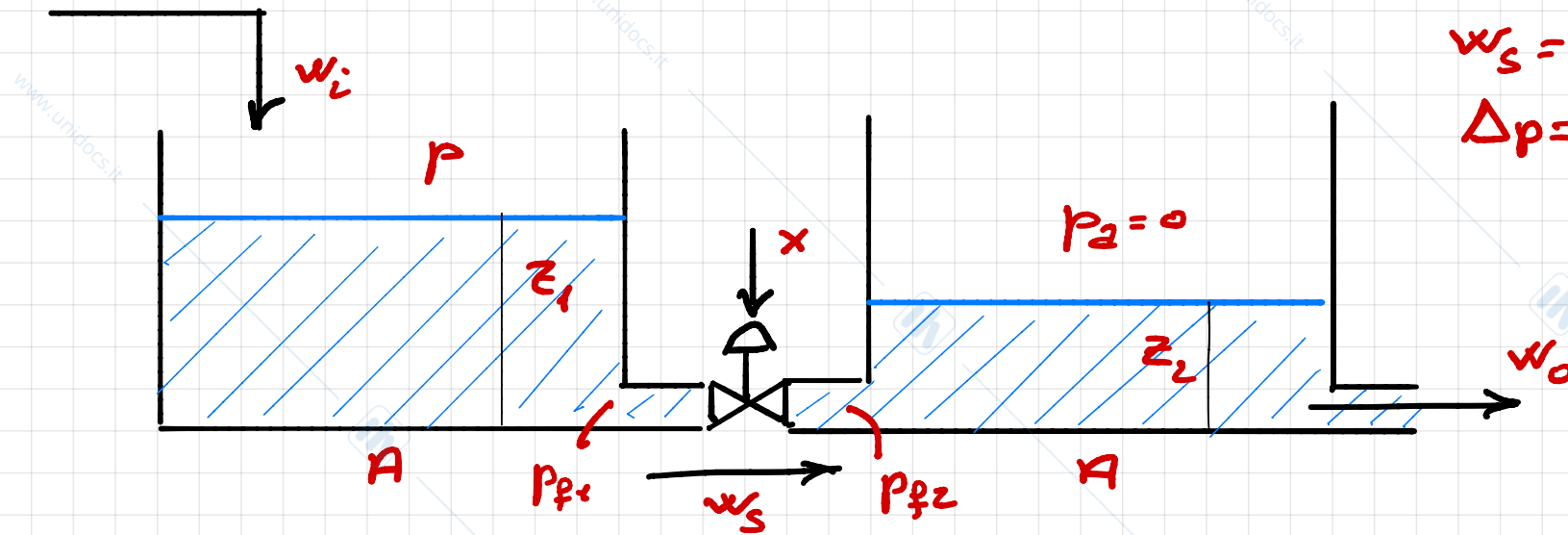
NON REALIZZABILE

$$C_w(s) = \begin{cases} \frac{s+\alpha}{\beta(1+s^2)}, & z \ll \frac{1}{\alpha} \\ \text{oppure} \\ \frac{\alpha}{\beta} = \frac{|x|}{\beta} \end{cases}$$

## ESELCIZIO 2

## IPOTESI

$$p > p_2$$
$$w_s = k \times \sqrt{\Delta p}$$
$$\Delta p = p_{f1} - p_{f2}$$



$x, w_o$  VARIABILI MANIPOLABILI

$w_i$  DISTURBO

# ① - MODELLO DINAMICO NON LINEARE

- SERBATOIO 1:  $\dot{z}_1 = \frac{1}{\rho A} (w_i - w_s)$

- SERBATOIO 2:  $\dot{z}_2 = \frac{1}{\rho A} (w_s - w_0)$

$$\Delta p = p_{f1} - p_{f2} = p + \rho g z_1 - \rho g z_2 = p + \rho g (z_1 - z_2)$$

$$w_s = kx \sqrt{p + \rho g (z_1 - z_2)}$$

$$\dot{z}_1 = \frac{1}{\rho A} w_i - \frac{kx}{\rho A} \sqrt{p + \rho g (z_1 - z_2)}$$

$$\dot{z}_2 = \frac{kx}{\rho A} \sqrt{p + \rho g (z_1 - z_2)} - \frac{1}{\rho A} w_0$$

②. EQUILIBRIO CON  $\bar{w}_i$  COSTANTE E  $\bar{z}_1, \bar{z}_2$  DATI

$$\bar{w}_s = \bar{w}_i = k\bar{x} \sqrt{p + \rho g(\bar{z}_1 - \bar{z}_2)} \Rightarrow \bar{x} = \frac{\bar{w}_i}{k \sqrt{p + \rho g(\bar{z}_1 - \bar{z}_2)}}$$

$$\bar{w}_0 = \bar{w}_i$$

ATTENZIONE! DEVE RISULTARE

$$\bar{x} \leq 1$$

### ③ - MODELLO LINEARIZZATO

$$\begin{cases} \delta \dot{z}_1(t) = -\alpha_1 \delta z_1(t) + \alpha_2 \delta z_2(t) - \alpha_3 \delta x(t) + \alpha_4 \delta w_i(t) \\ \delta \dot{z}_2(t) = \alpha_1 \delta z_1(t) - \alpha_2 \delta z_2(t) + \alpha_3 \delta x(t) - \alpha_5 \delta w_o(t) \end{cases}$$

$$\alpha_1 = \frac{k\bar{x}}{sA} \frac{s\gamma}{2\sqrt{p+s\gamma(\bar{z}_1-\bar{z}_2)}}$$

$$\alpha_2 = \frac{k\bar{x}}{sA} \frac{s\gamma}{2\sqrt{p+s\gamma(\bar{z}_1-\bar{z}_2)}} = \alpha_1$$

$$\alpha_3 = \frac{k}{sA} \sqrt{p+s\gamma(\bar{z}_1-\bar{z}_2)}$$

$$\alpha_4 = \alpha_5 = \frac{1}{sA}$$

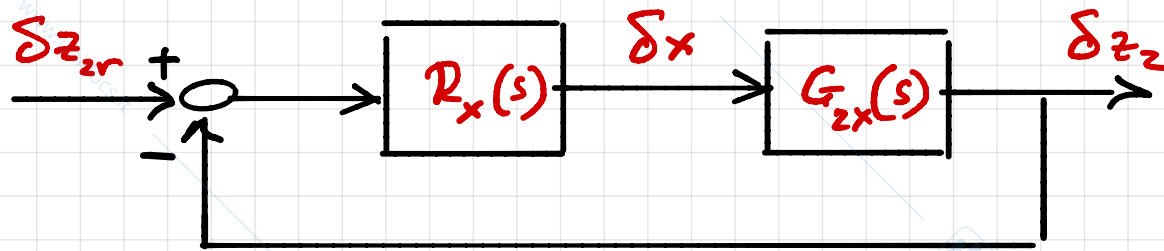
#### ④ - PROGETTO DI UN REGOLATORE PI DI $z_2$

$$A = \begin{bmatrix} -\alpha_1 & \alpha_1 \\ \alpha_1 & -\alpha_1 \end{bmatrix} \quad B = \begin{bmatrix} -\alpha_3 & 0 \\ \alpha_3 & -\alpha_4 \end{bmatrix} \quad C = I$$

$$G(s) = \frac{1}{(s+\alpha_1)^2 - \alpha_1^2} \begin{bmatrix} s+\alpha_1 & \alpha_1 \\ \alpha_1 & s+\alpha_1 \end{bmatrix} \begin{bmatrix} -\alpha_3 & 0 \\ \alpha_3 & -\alpha_4 \end{bmatrix} =$$
$$= \frac{1}{s(s+2\alpha_1)} \begin{bmatrix} -\alpha_3 s & -\alpha_1 \alpha_4 \\ \alpha_3 s & -\alpha_4 (s+\alpha_1) \end{bmatrix} = \begin{bmatrix} G_{1x} & G_{1w} \\ G_{2x} & G_{2w} \end{bmatrix}$$

- ④.1 PROGETTO CON VAR. DI CONTROLLO  $x$  SU  $G_{2x} = \frac{\alpha_3}{s+2\alpha_1}$
- ④.2 PROGETTO CON VAR. DI CONTROLLO  $w_0$  SU  $G_{2w} = \frac{-\alpha_4(s+\alpha_1)}{s(s+2\alpha_1)}$

# 4.1 - PROGETTO CON X



$$G_{zx}(s) = \frac{\alpha_3}{s + 2\alpha_1}$$

$$R_x(s) = \frac{K_p}{T_i} \frac{1 + sT_i}{s}$$

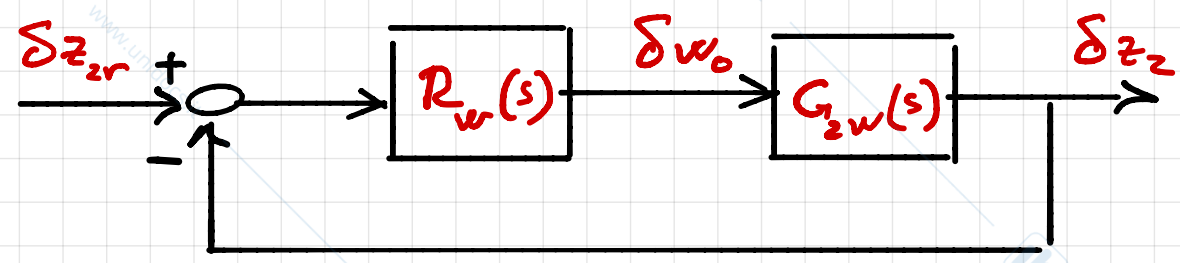
$$L_x(s) = \frac{\alpha_3 K_p}{2\alpha_1 T_i} \frac{1}{s}$$

$$K_p > 0$$

$$T_i = \frac{1}{2\alpha_1}$$

$$\left\{ \begin{array}{l} \omega_c = \frac{\alpha_3 K_p}{2\alpha_1 T_i} \\ \varphi_m = 90^\circ \end{array} \right.$$

# 4.2 - PROGETTO CON $v_0$



$$G_{zw}(s) = - \frac{\alpha_4 (s + \alpha_1)}{s (s + 2\alpha_1)}$$

$$R_w(s) = - K_p$$

$$K_p > 0$$

$$L_w(s) = \frac{\alpha_4 K_p}{2} \cdot \frac{1 + s/\alpha_1}{s (1 + s/2\alpha_1)}$$

5 - CONTROLLO DECENTRALIZZATO DI  $z_1, z_2$

