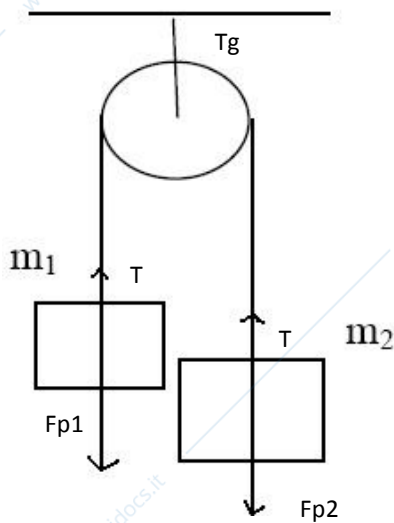


Dinamica es 1



m1:

$$T1 + Fp1 = m1 \cdot a1$$

Tenendo conto del SdR:

$$Fp1 - T1 = m1 \cdot a1$$

$$m1 \cdot g - T1 = m1 \cdot a1$$

m2:

$$T2 + Fp2 = m2 \cdot a2$$

Tenendo conto del SdR:

$$Fp2 - T2 = m2 \cdot a2$$

$$m2 \cdot g - T2 = m2 \cdot a2$$

$$T1 = T2 = T$$

$$A1 = a2 = a$$

$$m1 \cdot g - T = m1 \cdot a$$

$$m2 \cdot g - T = m2 \cdot a$$

$$T = m1(g - a)$$

$$m2 \cdot g - m1(g - a) = m \cdot a$$

$$T = m1(g - [(m1 - m2)/(m1 + m2)]g) = 2 \cdot [(m1 \cdot m2)/(m1 + m2)]g$$

$$a = [(m1 - m2)/(m1 + m2)]g$$

$$Tg + T + T = 0$$

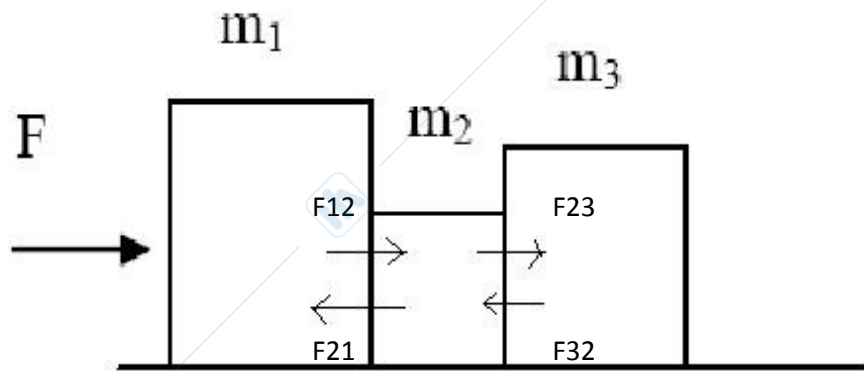
$$Fg = 2 \cdot Tg = 4 \cdot [(m1 \cdot m2)/(m1 + m2)]g$$

a) $a = [(m1 - m2)/(m1 + m2)]g$

b) $T = m1(g - [(m1 - m2)/(m1 + m2)]g) = 2 \cdot [(m1 \cdot m2)/(m1 + m2)]g$

c) $Fg = 2 \cdot Tg = 4 \cdot [(m1 \cdot m2)/(m1 + m2)]g$

Dinamica es 2



$m_1=45.2 \text{ Kg}$
 $m_2=22.8 \text{ Kg}$
 $m_3=34.3 \text{ kg}$
 $a=1.32 \text{ m/s}^2$
 $F_{12}=F_{21}$
 $F_{23}=F_{32}$

a) $F=(m_1+m_2+m_3)*a=135\text{N}$

$F_{23}=m_3*a$
 $F_{12}+F_{32}=m_2*a$
 $F+F_{21}=m_1*a$

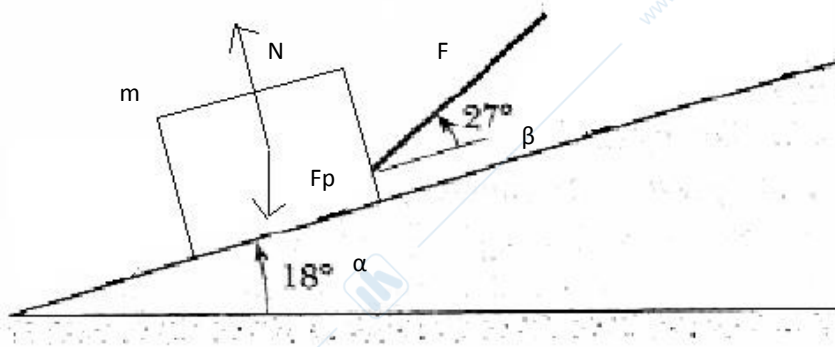
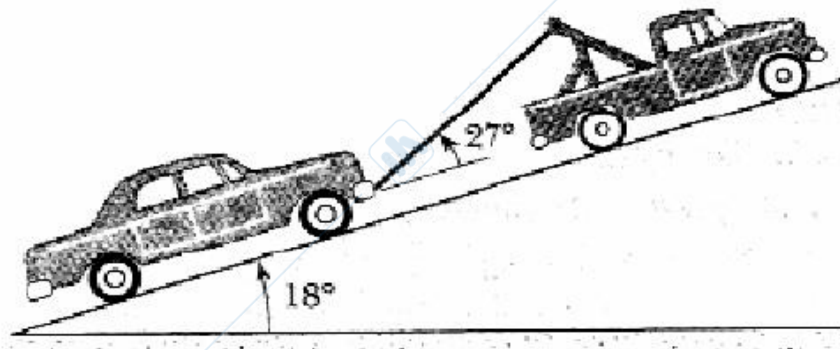
tenendo conto del SdR
 $F_{23}=m_3*a$
 $F_{12}-F_{32}=m_2*a$
 $F-F_{12}=m_1*a$

$F_{23}=m_3*a$
 $F_{12}-m_3*a=m_2*a$
 $F-(m_2+m_3)a=m_1*a$
 $F_{12}=a(m_2+m_3)$
 $F=(m_1+m_2+m_3)a$

b) $F_{23}=m_3*a=45.276 \text{ N}$

c) $F_{12}=a(m_2+m_3)=75.372 \text{ N}$

dinamica es 3



$m=1200 \text{ Kg}$
 $\alpha=18^\circ$
 $\beta=27^\circ$
carico di rottura del cavo= 4.6 kN
vuol dire che la $F_{\text{max}}=4.6 \text{ kN}$
 $F_p=m \cdot q$

$$m \cdot a = -F_p \cdot \sin \alpha + F \cos \beta$$

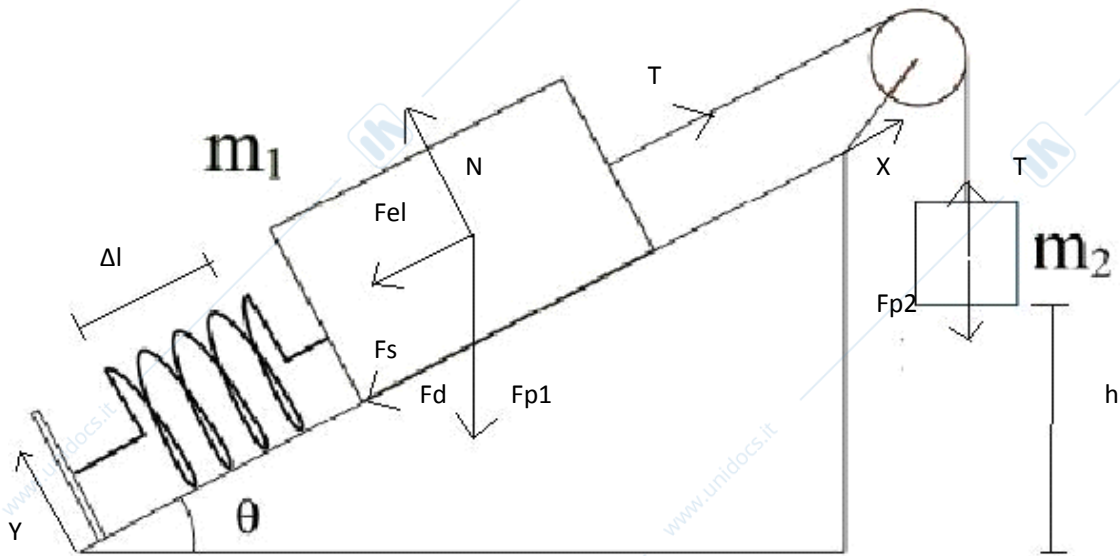
$$a = (F \cos \beta - F_p \cdot \sin \alpha) / m$$

$$S(t) = 1/2 a \cdot t^2$$

dinamica es 4

sabato 17 aprile 2010

9.58



$m_1 = 2 \text{ Kg}$
 $m_2 = 3 \text{ Kg}$
 $\theta = 30^\circ$
 $K_{el} = 30 \text{ N/m}$
 $\Delta l = 0.5 \text{ m}$
 $h = 10 \text{ m}$
 $\mu_d = 0.3$

IN EQUILIBRIO

a) $F_e = K_{el} \cdot \Delta l$	$m_2:$	$m_1:$	
$F_s = N \cdot \mu_s$			
$F_{p1} = m_1 \cdot g$	$F_{p2} - T = 0$	X: $T - F_e - F_s - F_{p1} \sin \theta = 0$	$m_1 \cdot g \cdot \cos \theta \cdot \mu_s = m_2 \cdot g - K_{el} \cdot \Delta l - m_1 \cdot g \cdot \sin \theta$
$F_{p2} = m_2 \cdot g$	$T = m_2 \cdot g$	Y: $N - F_{p1} \cos \theta = 0$	$N = m_1 \cdot g \cdot \cos \theta$

$$\mu_s = (m_2 \cdot g - K_{el} \cdot \Delta l - m_1 \cdot g \cdot \sin \theta) / (m_1 \cdot g \cdot \cos \theta)$$

b) TOLGO LA MOLLA
quindi non c'è più F_{el} e, visto che il sistema non è più in equilibrio si tiene conto di F_d al posto di F_s

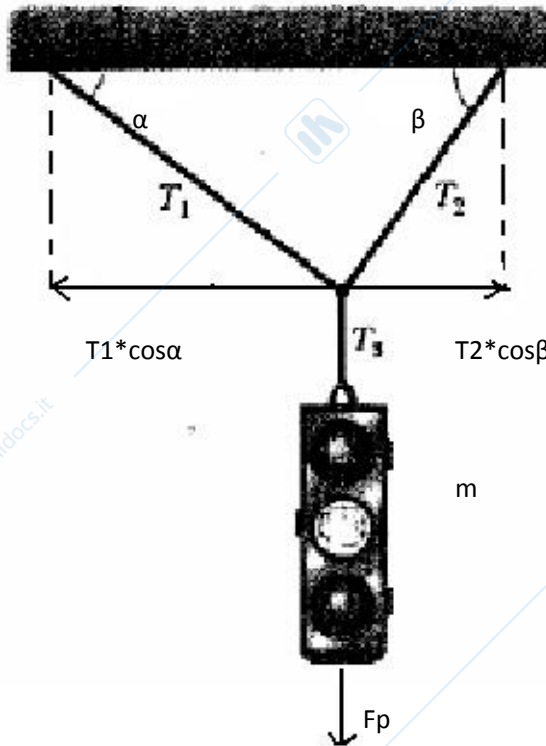
$F_d = N \cdot \mu_d$

$m_2:$	$m_1:$
$F_{p2} - T = m_2 \cdot a$	X: $T - F_e - F_s - F_{p1} \sin \theta = m_1 \cdot a$
$m_2 \cdot g - T = m_2 \cdot a$	Y: $N - F_{p1} \cos \theta = 0$
$T = m_2(g - a)$	$N = m_1 \cdot g \cdot \cos \theta$

$m_2(g - a) - K_{el} \cdot \Delta l - m_1 \cdot g \cdot \cos \theta \cdot \mu_d m_2 \cdot g - m_1 \cdot g \cdot \sin \theta = m_1 \cdot a$
 $m_2 g - K_{el} \cdot \Delta l - m_1 \cdot g \cdot \cos \theta \cdot \mu_d m_2 \cdot g - m_1 \cdot g \cdot \sin \theta = (m_1 + m_2) \cdot a$
 $a = (m_2 g - K_{el} \cdot \Delta l - m_1 \cdot g \cdot \cos \theta \cdot \mu_d m_2 \cdot g - m_1 \cdot g \cdot \sin \theta) / (m_1 + m_2) = 2.90 \text{ m/s}^2$

$h = \frac{1}{2} a t^2$ $t^2 = 2h/a$ $t = 2.63 \text{ s}$

dinamica es 5



$$\alpha = 37^\circ$$

$$\beta = 53^\circ$$

$$m = 12.74 \text{ Kg}$$

$$T_3 - F_p = 0 \quad T_3 = m \cdot g = 125 \text{ N}$$

$$X: -T_1 \cdot \cos \alpha + T_2 \cdot \cos \beta = 0$$

$$Y: T_1 \cdot \sin \alpha + T_2 \cdot \sin \beta = T_3$$

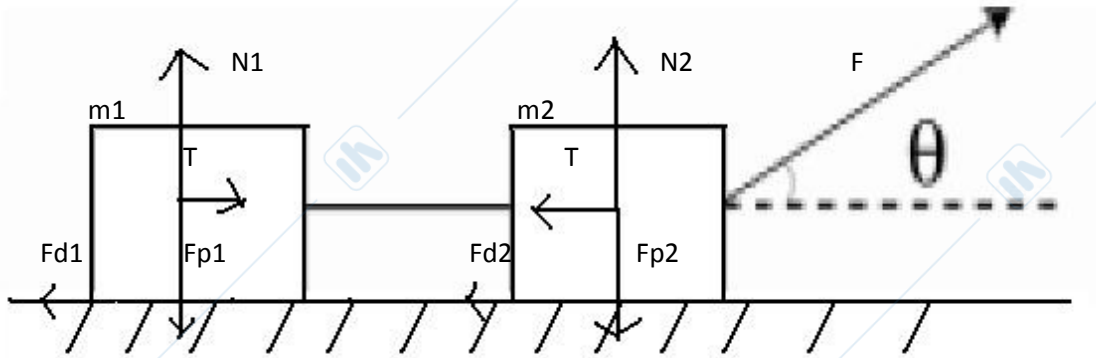
$$T_1 = \frac{T_2 \cdot \cos \beta}{\cos \alpha}$$

$$(T_2 \cdot \cos \beta / \cos \alpha) \cdot \sin \alpha + T_2 \cdot \sin \beta = T_3$$

$$T_2 = T_3 / ((\cos \beta \cdot \sin \alpha / \cos \alpha) + \sin \beta) = 99.8 \text{ N}$$

$$T_1 = 75.2 \text{ N}$$

dinamica es 6



$m_1=5 \text{ Kg}$
 $m_2=10 \text{ Kg}$
 $\theta=30^\circ$
 $\mu_d=0.45$
 $F=100 \text{ N}$

$F_{d1}=\mu_d \cdot N_1$
 $F_{d2}=\mu_d \cdot N_2$

m1:

$$\begin{aligned} \text{X: } m_1 \cdot a &= T - F_{d1} & m_1 \cdot a &= T - m_1 \cdot g \cdot \mu_d & T &= m_1(a + g \cdot \mu_d) \\ \text{Y: } N_1 - F_{p1} &= 0 & N_1 &= F_{p1} = m_1 \cdot g \end{aligned}$$

m2:

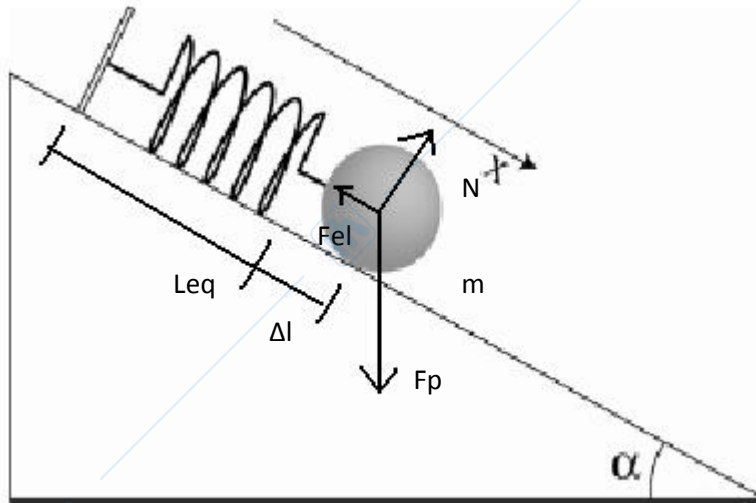
$$\begin{aligned} \text{X: } m_2 \cdot a &= F \cdot \cos \theta - T - F_{d2} & m_2 \cdot a &= F \cdot \cos \theta - T - (m_2 \cdot g - F \cdot \sin \theta) \cdot \mu_d \\ \text{Y: } N_2 + F \cdot \sin \theta - F_{p2} &= 0 & N_2 &= m_2 \cdot g - F \cdot \sin \theta \end{aligned}$$

$$\begin{aligned} m_2 \cdot a &= F \cdot \cos \theta - T - (m_2 \cdot g - F \cdot \sin \theta) \cdot \mu_d \\ T &= m_1(a + g \cdot \mu_d) \end{aligned}$$

$$\begin{aligned} m_2 \cdot a &= F \cdot \cos \theta - m_1(a + g \cdot \mu_d) - (m_2 \cdot g - F \cdot \sin \theta) \cdot \mu_d \\ (m_1 + m_2) \cdot a &= F \cdot \cos \theta + m_1 g \cdot \mu_d - (m_2 \cdot g - F \cdot \sin \theta) \cdot \mu_d \\ a &= (F \cdot \cos \theta + m_1 g \cdot \mu_d - (m_2 \cdot g - F \cdot \sin \theta) \cdot \mu_d) / (m_1 + m_2) = 2.86 \text{ m/s}^2 \end{aligned}$$

$$T = 36.4 \text{ N}$$

dinamica es 7



$$\alpha = 40^\circ$$

$$K_{el} = 500 \text{ N/m}$$

$$m = 5 \text{ Kg}$$

$$\Delta l = 10 \text{ cm}$$

$$F_{el} = L \cdot K_{el}$$

$$F_p = m \cdot g$$

a) SISTEMA IN EQUILIBRIO $\Rightarrow a=0$

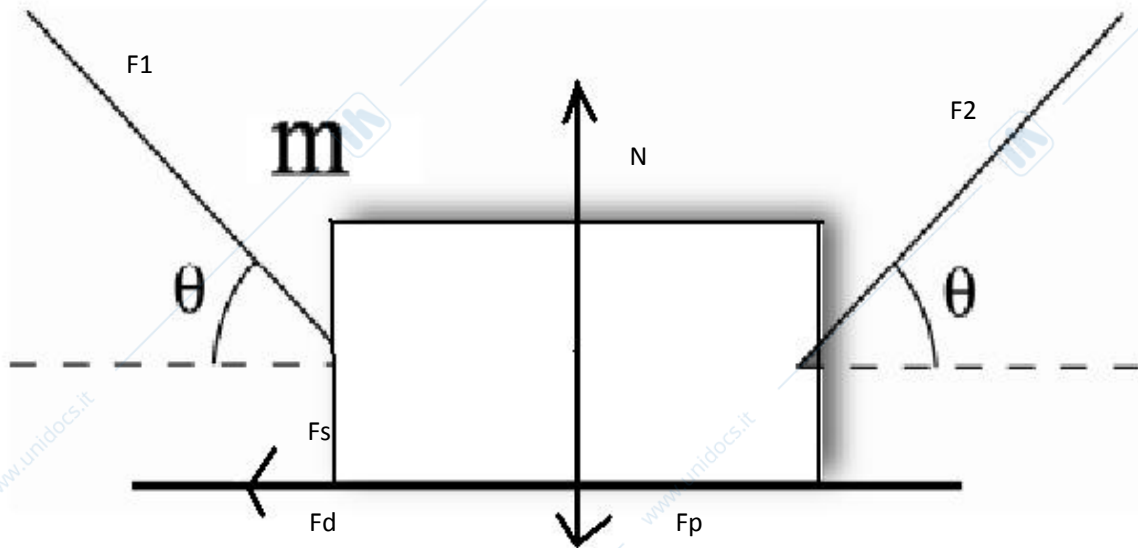
$$F_{el} - F_p \cdot \sin \alpha = 0$$

$$L_{eq} \cdot K_{el} = m \cdot g \cdot \sin \alpha$$

$$L_{eq} = (m \cdot g \cdot \sin \alpha) / K_{el}$$

b) molla in posizione $L_{eq} + \Delta l$

dinamica es 8



$$\begin{aligned} \theta &= 60^\circ \\ \mu_s &= 0.45 \\ \mu_d &= 0.35 \\ F_p &= m \cdot g \\ F_d &= N \cdot \mu_d \end{aligned}$$

a) scopro la forza più conveniente

F1:

$$X: F1 \cdot \cos\theta - F_s = 0$$

$$Y: N - F_p - F1 \cdot \sin\theta = 0$$

$$F1 \cdot \cos\theta - (F1 \cdot \sin\theta + m \cdot g) \cdot \mu_s = 0$$

$$N = m \cdot g + F1 \cdot \sin\theta$$

$$F1 \cdot (\cos\theta - \sin\theta \cdot \mu_s) = m \cdot g \cdot \mu_s$$

$$F1 = (m \cdot g \cdot \mu_s) / (\cos\theta - \sin\theta \cdot \mu_s) = 1199.6 \text{ N}$$

F2:

$$X: F2 \cdot \cos\theta - F_s = 0$$

$$Y: N - F_p + F2 \cdot \sin\theta = 0$$

$$F2 \cdot \cos\theta - (m \cdot g - F2 \cdot \sin\theta) \cdot \mu_s = 0$$

$$N = m \cdot g - F2 \cdot \sin\theta$$

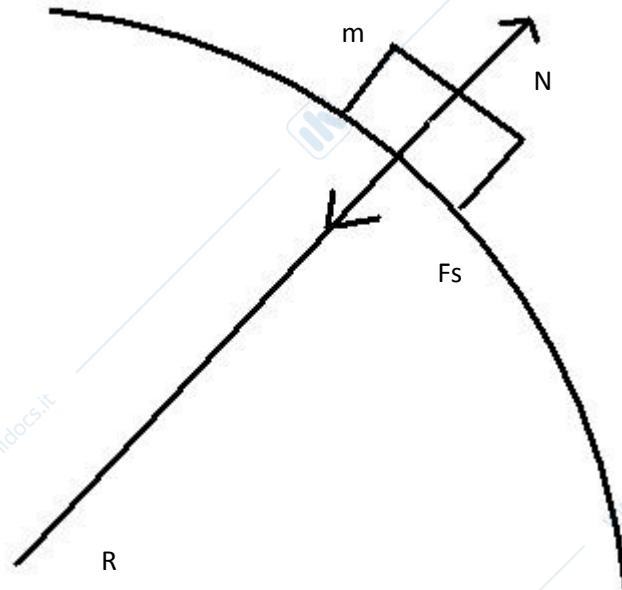
$$F2 \cdot (\cos\theta + \sin\theta \cdot \mu_s) = m \cdot g \cdot \mu_s$$

$$F2 = (m \cdot g \cdot \mu_s) / (\cos\theta + \sin\theta \cdot \mu_s) = 148.7 \text{ N}$$

b) lavoro L per spostare la cassa di Δl

$$L = F \cdot \Delta l = 1487 \text{ J}$$

dinamica es 9



$$m=1500 \text{ Kg}$$

$$R=35 \text{ m}$$

$$N=(V^2/R)*m$$

$$F_s=\mu_s*N$$

a) SISTEMA IN EQUILIBRIO $\Rightarrow a=0$

$$\mu_s=0.5$$

$$V=?$$

$$m*V^2/R - \mu_s m * g = 0$$

$$V^2 = \mu_s * R * g$$

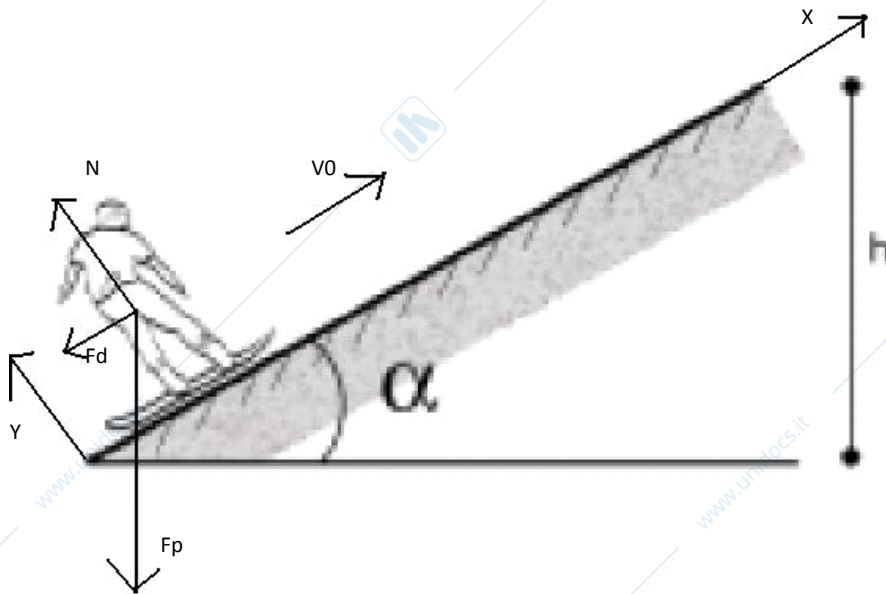
$$V = 13.1 \text{ m/s}$$

b) $V_{\text{max}} = 8 \text{ m/s}$
 $\mu_s = ?$

$$V^2 = \mu_s * R * g$$

$$\mu_s = v^2 / (R * g) = 0.19$$

dinamica es 10



$$\begin{aligned} v_0 &= 20 \text{ m/s} \\ \mu_d &= 0.2 \\ \alpha &= 15^\circ \\ F_d &= N \cdot \mu_d \\ F_p &= m \cdot g \end{aligned}$$

a) LEGGE ORARIA

$$\begin{aligned} X: m \cdot a &= -F_d - F_p \cdot \sin \alpha \\ Y: F_p \cdot \cos \alpha &= N \end{aligned}$$

$$\begin{aligned} m \cdot a &= -\mu_d \cdot m \cdot g \cdot \cos \alpha - m \cdot g \cdot \sin \alpha \\ a &= -g(\sin \alpha + \mu_d \cdot \cos \alpha) \end{aligned}$$

$$S(t) = v_0 \cdot t + \frac{1}{2} a \cdot t^2$$

$$S(t) = v_0 \cdot t - \frac{1}{2} g(\sin \alpha + \mu_d \cdot \cos \alpha) \cdot t^2$$

b) altezza massima hmax e tempo t necessario per raggiungerla
si ha altezza massima quando V(t)=0

$$V(t) = dx/dt$$

$$V(t) = v_0 - g(\sin \alpha - \mu_d \cdot \cos \alpha) \cdot t$$

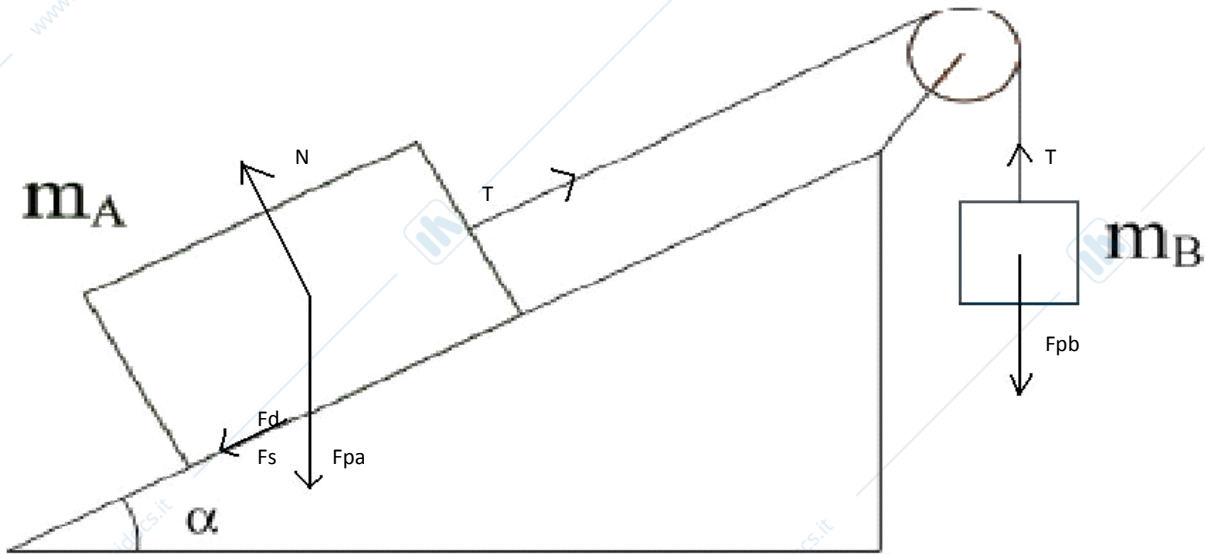
$$v_0 - g(\sin \alpha - \mu_d \cdot \cos \alpha) \cdot t = 0$$

$$t = v_0 / g(\sin \alpha - \mu_d \cdot \cos \alpha) = 4.515 \text{ s}$$

$$S(t_{\max}) = S_{\max} \Rightarrow S_{\max} = v_0 \cdot t_{\max} - \frac{1}{2} g(\sin \alpha + \mu_d \cdot \cos \alpha) \cdot t_{\max}^2 = 45.15 \text{ m/s}$$

$$h_{\max} = S_{\max} \cdot \sin \alpha = 11.67 \text{ m}$$

dinamica es 11



$m_A = 42.6 \text{ Kg}$
 $m_B = 13.2 \text{ Kg}$
 $\alpha = 42^\circ$
 $\mu_s = 0.56$
 $\mu_d = 0.25$

a) SISTEMA IN EQUILIBRIO:

si tiene conto di F_s e non di F_d nel calcolo

m_A :

$$\begin{aligned} X: T - F_s - F_{pa} \sin \alpha &= m_A a \\ Y: N - F_{pa} \cos \alpha &= 0 \end{aligned}$$

$$\begin{aligned} m_B (q - a) - m_A q \cos \alpha \mu_s - m_A q \sin \alpha &= m_A a \\ N &= m_A q \cos \alpha \end{aligned}$$

m_B :

$$F_{pb} - T = m_B a$$

$$T = m_B q - m_B a$$

$$T = m_B (q - a)$$

$$\begin{aligned} m_B q - m_A q \cos \alpha \mu_s - m_A q \sin \alpha &= (m_A + m_B) a \\ a &= (m_B q - m_A q \cos \alpha \mu_s - m_A q \sin \alpha) / (m_A + m_B) = -5.8 \text{ m/s} \end{aligned}$$

e quindi se si pone il sistema in equilibrio il corpo comincerà a scendere verso il basso

b) IL CORPO A SALE LUNGO IL PIANO

si tiene conto di F_d che scende lungo il piano

m_A :

$$\begin{aligned} X: T - F_d - F_{pa} \sin \alpha &= m_A a \\ Y: N - F_{pa} \cos \alpha &= 0 \end{aligned}$$

$$\begin{aligned} m_B (q - a) - m_A q \cos \alpha \mu_d - m_A q \sin \alpha &= m_A a \\ N &= m_A q \cos \alpha \end{aligned}$$

m_B :

$$F_{pb} - T = m_B a$$

$$T = m_B q - m_B a$$

$$T = m_B (q - a)$$

$$\begin{aligned} m_B q - m_A q \cos \alpha \mu_d - m_A q \sin \alpha &= (m_A + m_B) a \\ a &= (m_B q - m_A q \cos \alpha \mu_d - m_A q \sin \alpha) / (m_A + m_B) \end{aligned}$$

c) IL CORPO A SCENDE LUNGO IL PIANO

si tiene conto di F_d che sale lungo il piano

m_A :

$$\begin{aligned} X: T + F_d - F_{pa} \sin \alpha &= m_A a \\ Y: N - F_{pa} \cos \alpha &= 0 \end{aligned}$$

$$\begin{aligned} m_B (q - a) + m_A q \cos \alpha \mu_d - m_A q \sin \alpha &= m_A a \\ N &= m_A q \cos \alpha \end{aligned}$$

m_B :

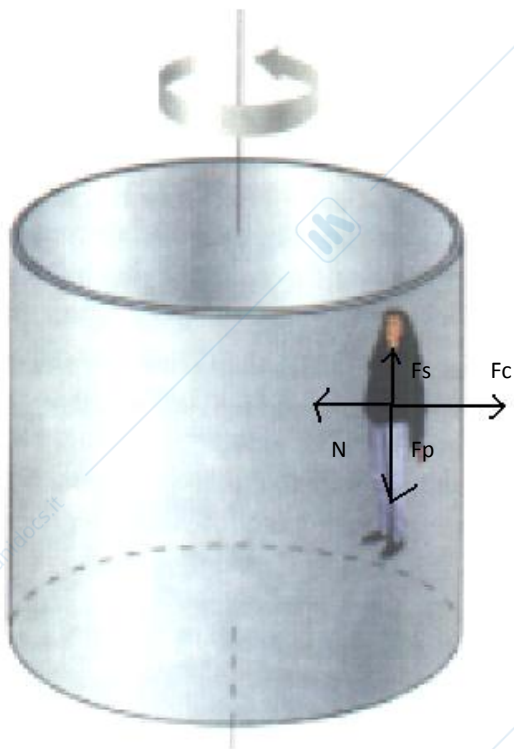
$$-F_{pb} + T = m_B a$$

$$T = -m_B q + m_B a$$

$$T = m_B (a - q)$$

$$\begin{aligned} m_B q + m_A q \cos \alpha \mu_d - m_A q \sin \alpha &= (m_A - m_B) a \\ a &= (m_B q + m_A q \cos \alpha \mu_d - m_A q \sin \alpha) / (m_A - m_B) \end{aligned}$$

dinamica es 12



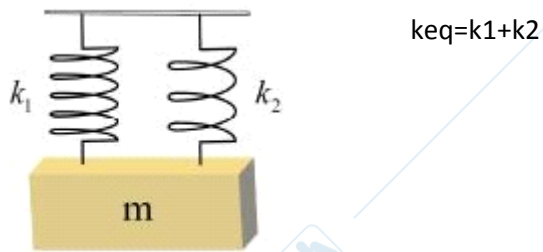
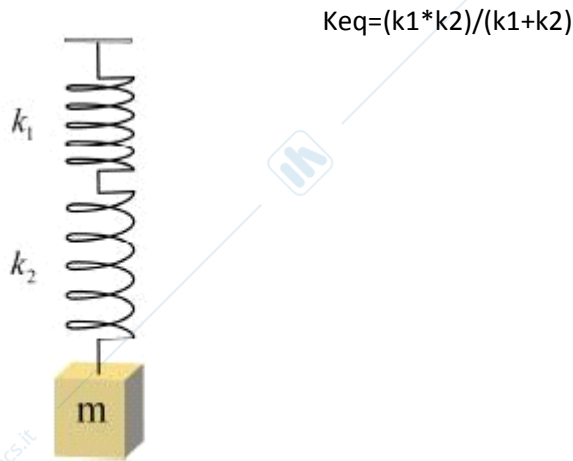
$$\begin{aligned} F_p &= m \cdot g \\ F_s &= N \cdot \mu_s \\ N - F_c &= 0 \Rightarrow N = F_c \\ F_c &= m \cdot \omega^2 \cdot R \\ \omega &= 2\pi / T \end{aligned}$$

per avere un sistema in equilibrio:

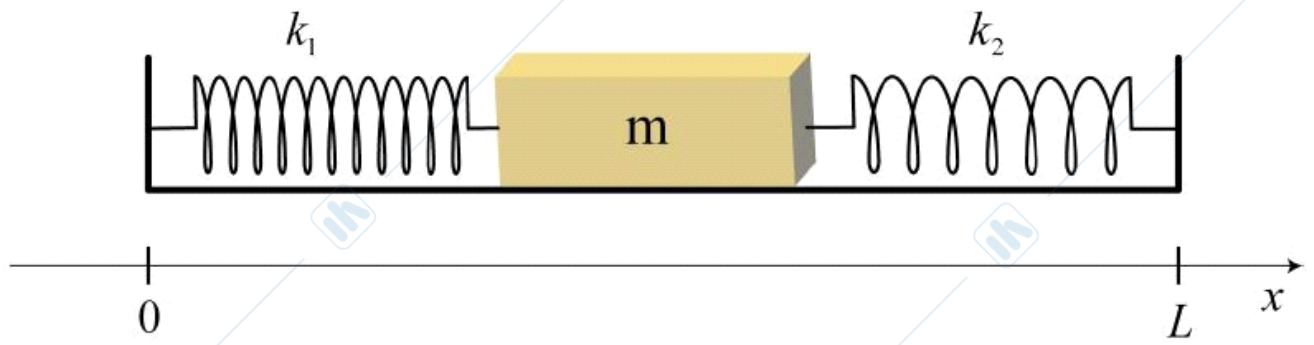
$$F_p = F_c \cdot \mu_s$$

$$\begin{aligned} m \cdot g &= m \omega^2 \cdot R \cdot \mu_s \\ T^2 &= (4\pi^2 \cdot R \cdot \mu_s) / g \end{aligned}$$

dinamica es 13



dinamica es 14



a) SISTEMA IN EQUILIBRIO

per avere un sistema in equilibrio deve essere soddisfatta l'equazione: $k_1 \cdot \Delta L_1 = k_2 \cdot \Delta L_2$